

Quick
Check
6.3.7

Factor completely.

$$90m^2 - 19m - 90$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

☐ A. $90m^2 - 19m - 90 = \blacksquare$ (Factor completely.)

☐ B. The polynomial is prime.

factors that give 90

1, 90
2, 45
3, 30
5, 18
6, 15
9, 10

$$(9x - 10)(10x + 9)$$

$$-100 + 81 = -19.$$

$$\begin{array}{r} 8100 \\ \times -19 \\ \hline \end{array}$$

$$90m^2 + 81m - 100m - 90$$

$$9m(10m + 9) - 10(10m + 9)$$

$$(10m + 9)(9m - 10)$$

$$1, 8100$$

$$2, 4050$$

$$3, 2700$$

$$4, 2025$$

$$5, 1620$$

$$6, 1350$$

$$8, 1215$$

$$9, 1080$$

$$10, 810$$

$$12, 675$$

$$15, 540$$

$$18, 450$$

$$20, 405$$

$$25, 324$$

$$27, 300$$

$$30, 270$$

$$36, 225$$

$$45, 180$$

$$50, 162$$

$$96 \leftarrow 54, 150$$

$$75 \leftarrow 60, 135$$

$$81, 100$$

$$90, 90$$

Quick
Check
6.3.15

Factor the trinomial completely using the trial and error method.

$$-14y^2 + 125y + 9$$

$$-14y^2 + 125y + 9 = \square$$

factor out -1:

$$-(14y^2 - 125y - 9)$$

factors of 14

1, 14

2, 7

factors of 9

1, 9

3, 3

$$(y-9)(14y+1)$$

$-126 + 1 = -125$ right #, wrong sign

$$\boxed{-(y+9)(14y-1)}$$

$$-(14y^2 - 125y - 9)$$

$$= -[14y^2 - 126y + y - 9]$$

$$= -[14y(y-9) + (y-9)]$$

$$= \boxed{-(y-9)(14y+1)}$$

$$\begin{array}{cc} & -126 \\ -126 & +1 \\ & -125 \end{array}$$

6.3.35

Factor completely.

$$35x^2 - 82x + 48$$

$$35x^2 - 82x + 48 = (7x - 8)(5x - 6)$$

Guess & check

$$(5x \quad \quad \quad)(7x \quad \quad \quad)$$

$$(5x - 8)(7x - 6)$$

$$-30 - 56 \times$$

$$(5x - 6)(7x - 8)$$

$$-40 - 42 \checkmark$$

$$\begin{array}{r} 1680 \\ \times -82 \\ \hline \end{array}$$

$$35x^2 - 40x - 42x + 48$$

$$= 5x(7x - 8) - 6(7x - 8)$$

$$= (7x - 8)(5x - 6)$$

1, 1680

2, 840

3, 560

4, 420

5, 336

6, 280

7, 240

8, 210

10, 168

12, 140

14, 120

15, 112

16, 105

20, 84

21, 80

24, 70

28, 60

30, 56

35, 48

40, 42

6.3.35

Factor completely.

$$33x^2 - 46x + 16$$

$$33x^2 - 46x + 16 = \boxed{(11x+3)(3x-3)}$$

1, 33
and
1, 16
2, 8
4, 4

$$(11x-4)(3x-4)$$

$$33x^2 - 44x - 12x + 16$$

$$-56x \text{ NO}$$

$$(11x-1)(3x-16)$$

$$-3x - 176x \text{ NO}$$

$$(11x-16)(3x-1)$$

$$-11x - 48x = -59x \text{ NO}$$

$$(33x-4)(x-4)$$

$$-4x - 132x \text{ NO}$$

$$(33x-1)(x-16)$$

$$-x - 528x \text{ NO}$$

$$(33x-16)(x-1)$$

$$-16 - 33 = -49 \text{ NO}$$

$$\boxed{(11x-8)(3x-2)}$$

$$-24x - 22x = -46x$$

$$\begin{array}{r} 528 \\ \times -46 \\ \hline \end{array}$$

1, 528
2, 264
3, 176
4, 132
6, 88
8, 66
11, 48
12, 44
16, 33
22, 24. ✓

$$33x^2 - 22x - 24x + 16$$

$$11x(3x-2) - 8(3x-2)$$

$$\boxed{(11x-8)(3x-2)}$$

6.3.43

Factor the trinomial completely.

$$84s^2 - 38sr - 70r^2$$

$$84s^2 - 38sr - 70r^2 = \square$$

GCF first

$$= 2(42s^2 - 19sr - 35r^2)$$

Factors
of
42:
1, 42
2, 21
3, 14
6, 7

↪ 1, 35
5, 7 Factors
of 35

Guess and check

$$(6s - 5r)(7s - 7r)$$

has GCF X

$$(6s - 7r)(7s + 5r)$$

$$30rs - 49rs = -19rs \checkmark$$

$$= \boxed{2(6s - 7r)(7s + 5r)}$$

6.3.85

Factor.

$$25c^2 + 29c + 9$$

Select the correct choice below and fill in any answer boxes within your choice.

☐ A. $25c^2 + 29c + 9 = \blacksquare$

☒ B. The expression is prime.

It's prime because $25c^2$ and 9 are perfect squares, but

$$(5c+3)(5c+3)$$

gives $25c^2 + 15c + 15c + 9$

$$= 25c^2 + 30c + 9$$

which has the wrong middle term.